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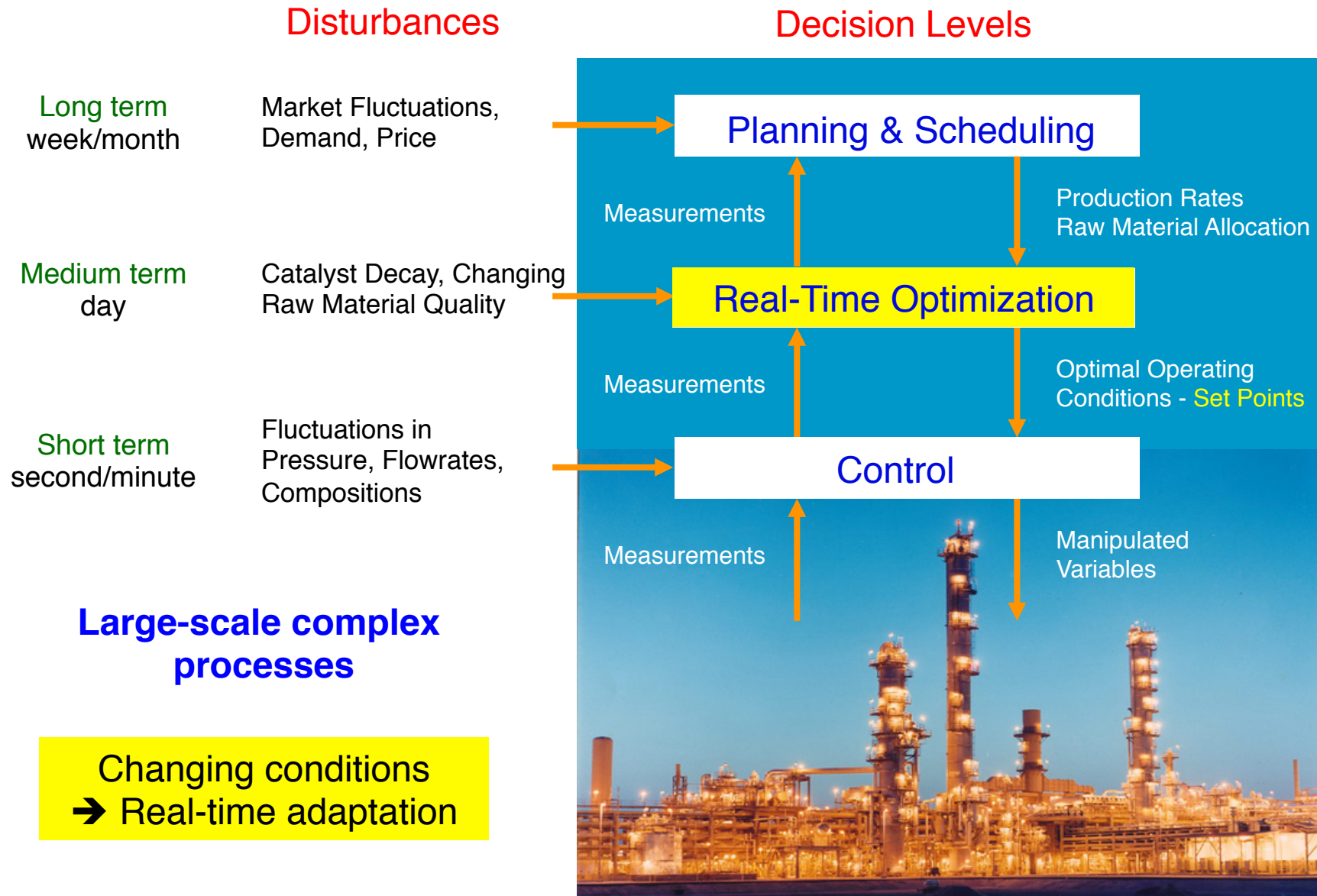


# Real-Time Optimization of Chemical Processes

**Dominique Bonvin**, Grégory François and Gene Bunin  
Laboratoire d'Automatique  
EPFL, Lausanne

SFGP, Lyon 2013

# Real-Time Optimization of a Continuous Plant

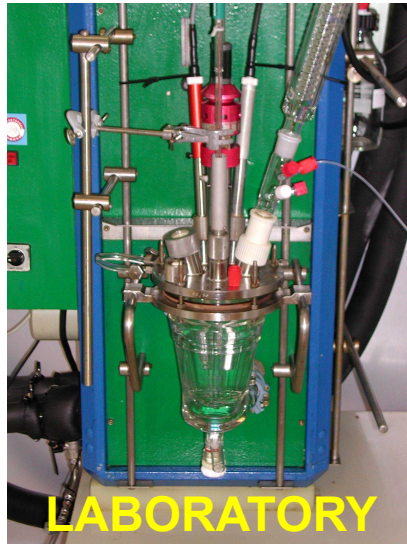


# Optimization of a Discontinuous Plant

RECIPE

BATCH PLANT

PRODUCTS



## Differences in Equipment and Scale

- mass- and heat-transfer characteristics
- surface-to-volume ratios
- operational constraints

Scale-up



## Production Constraints

- meet product specifications
- meet safety and environmental constraints
- adhere to equipment constraints

Different conditions → Run-to-run adaptation

# Outline

## What is real-time optimization

- **Goal:** Optimal plant operation
- **Tool:** Model-based numerical optimization, experimental optimization
- Key feature: **use of real-time measurements**

## Real-time optimization framework

- Three approaches
- Key issues: **Which measurements? How to best exploit them?**
- Simulated comparison

## Experimental case studies

- Fuel-cell stack
- Batch polymerization

# Static Optimization Problem

Optimize the steady-state **performance** of a (dynamic) process while satisfying a number of operating **constraints**

## Plant

$$\begin{aligned} \min_{\mathbf{u}} \quad & \Phi_p(\mathbf{u}) := \phi_p(\mathbf{u}, \mathbf{y}_p) \\ \text{s. t.} \quad & \mathbf{G}_p(\mathbf{u}) := \mathbf{g}_p(\mathbf{u}, \mathbf{y}_p) \leq \mathbf{0} \end{aligned}$$

Optimal plant operation

Inputs  $\mathbf{u}$  ?  
(set points)



Plant  
Outputs  $\mathbf{y}_p$

## Model-based Optimization

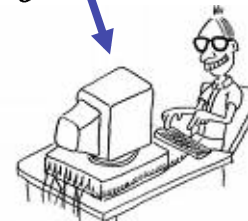
$$\begin{aligned} \mathbf{F}(\mathbf{u}, \mathbf{y}, \boldsymbol{\theta}) &= \mathbf{0} \\ \min_{\mathbf{u}} \quad & \Phi(\mathbf{u}) := \phi(\mathbf{u}, \mathbf{y}) \\ \text{s. t.} \quad & \mathbf{G}(\mathbf{u}) := \mathbf{g}(\mathbf{u}, \mathbf{y}) \leq \mathbf{0} \end{aligned}$$

NLP

Model-based  
numerical optimization

Model  
Parameters  $\boldsymbol{\theta}$  ?

Inputs  $\mathbf{u}$  ?  
(set points)



Predicted  
Outputs  $\mathbf{y}$

# Dynamic Optimization Problem

Optimize the dynamic **performance** of a (dynamic) process while satisfying a number of operating **constraints**

## Plant

$$\min_{\mathbf{u}[0,t_f]} \Phi := \phi(\mathbf{x}_p(t_f))$$

$$\text{s. t.} \quad \mathbf{S}(\mathbf{x}_p, \mathbf{u}) \leq \mathbf{0}$$

$$\mathbf{T}(\mathbf{x}_p(t_f)) \leq \mathbf{0}$$

Optimal plant operation



## Model-based Optimization

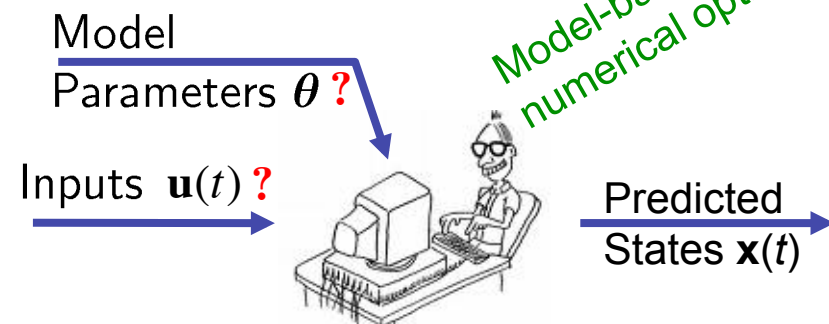
$$\min_{\mathbf{u}[0,t_f]} \Phi := \phi(\mathbf{x}(t_f), \boldsymbol{\theta})$$

$$\text{s. t.} \quad \dot{\mathbf{x}} = \mathbf{F}(\mathbf{x}, \mathbf{u}, \boldsymbol{\theta}) \quad \mathbf{x}(0) = \mathbf{x}_0$$

$$\mathbf{S}(\mathbf{x}, \mathbf{u}, \boldsymbol{\theta}) \leq \mathbf{0}$$

$$\mathbf{T}(\mathbf{x}(t_f), \boldsymbol{\theta}) \leq \mathbf{0}$$

Model-based  
numerical optimization





# Run-to-Run Optimization of a Batch Plant



Batch plant with  
finite terminal time

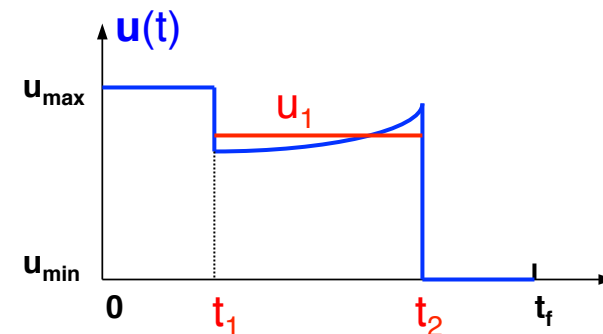
$$\begin{aligned} \min_{\mathbf{u}[0, t_f]} \quad & \Phi := \phi(\mathbf{x}(t_f), \boldsymbol{\theta}) \\ \text{s. t.} \quad & \dot{\mathbf{x}} = \mathbf{F}(\mathbf{x}, \mathbf{u}, \boldsymbol{\theta}) \quad \mathbf{x}(0) = \mathbf{x}_0 \\ & \mathbf{S}(\mathbf{x}, \mathbf{u}, \boldsymbol{\theta}) \leq \mathbf{0} \\ & \mathbf{T}(\mathbf{x}(t_f), \boldsymbol{\theta}) \leq \mathbf{0} \end{aligned}$$

## Input Parameterization

$$\mathbf{u}[0, t_f] = \mathbf{U}(\boldsymbol{\pi})$$



Batch plant  
viewed as a static map



$$\begin{aligned} \min_{\boldsymbol{\pi}} \quad & \Phi(\boldsymbol{\pi}, \boldsymbol{\theta}) \\ \text{s. t.} \quad & \mathbf{G}(\boldsymbol{\pi}, \boldsymbol{\theta}) \leq \mathbf{0} \end{aligned}$$

NLP



# Outline

## What is real-time optimization

- Goal: Optimal plant operation
- Tool: Model-based numerical optimization, experimental optimization
- Key feature: use of real-time measurements

## Real-time optimization framework

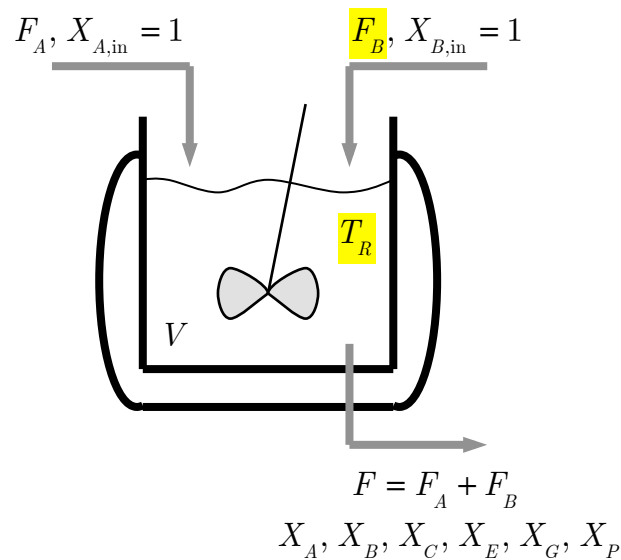
- Three approaches
- Key issues: **Which measurements? How to best exploit them?**
- Simulated comparison

## Experimental case studies

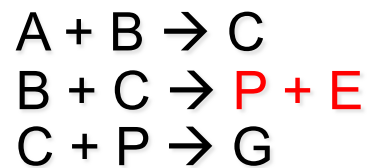
- Fuel-cell stack
- Batch polymerization

# Example of Plant-Model Mismatch

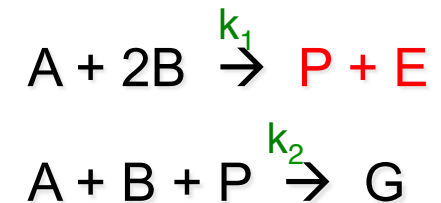
## Williams-Otto reactor



### 3-reaction system



### 2-reaction model



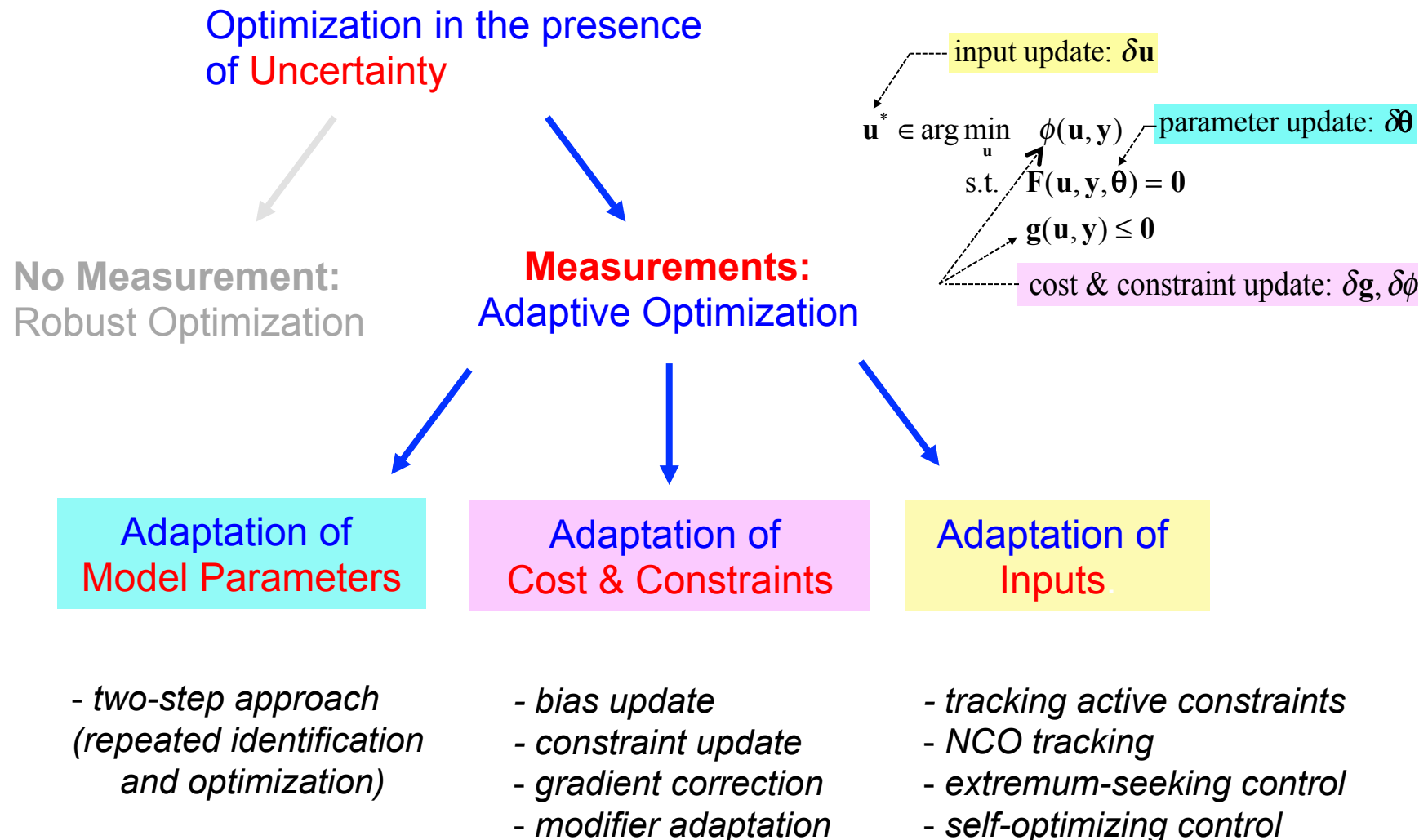
**Objective:** maximize operating profit

### Model

- 4<sup>th</sup>-order model
- 2 inputs
- 2 adjustable parameters ( $k_{10}, k_{20}$ )

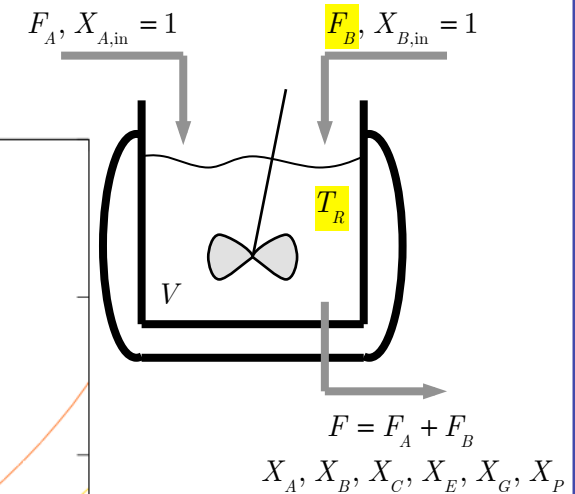
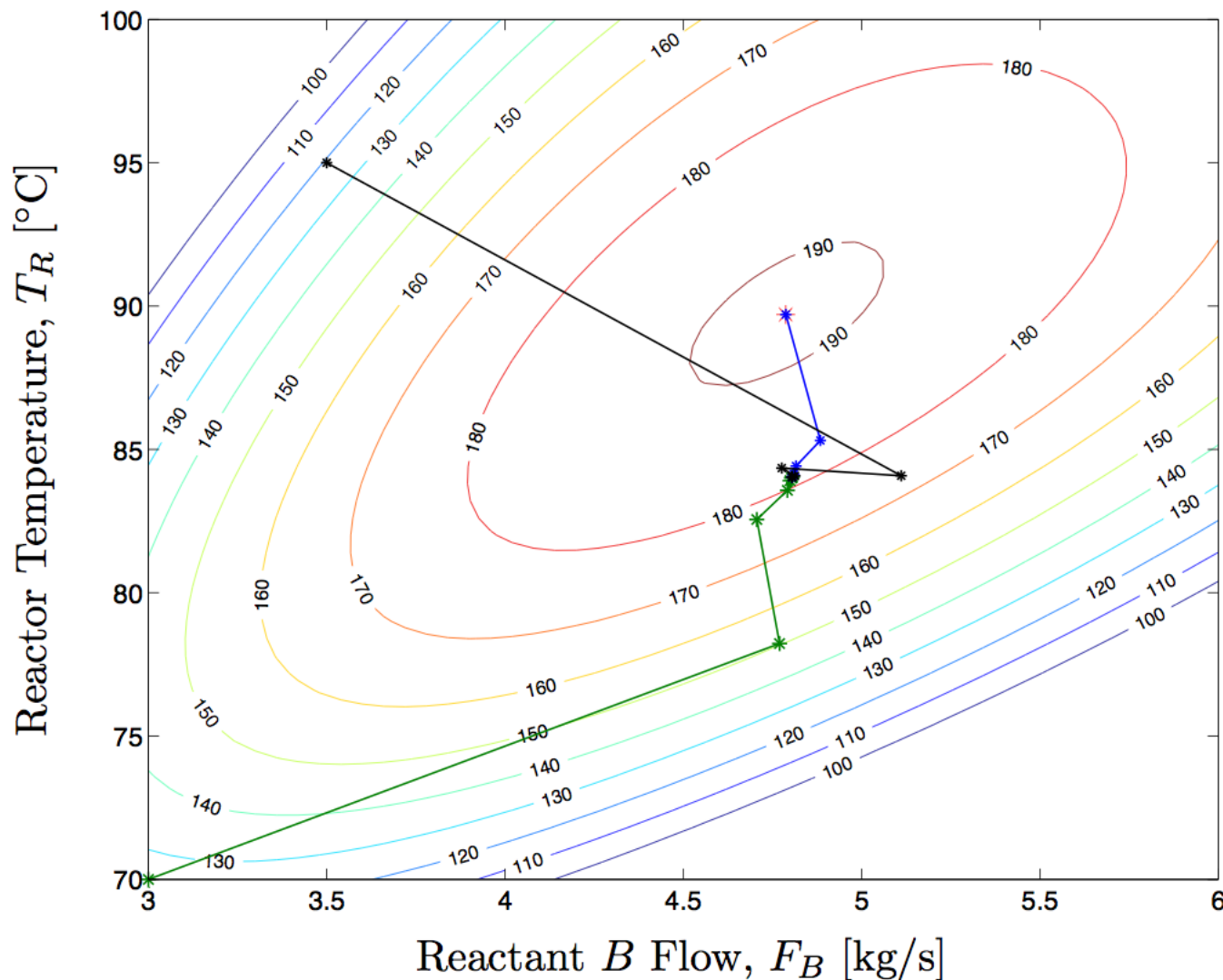
# Three RTO Approaches

## How to best exploit the measurements?



# 1. Adaptation of Model Parameters

## Two-step approach



### Williams-Otto Reactor

- 4<sup>th</sup>-order model
- 2 inputs
- 2 adjustable par.

Does not  
converge to plant  
optimum

# Two-step approach

## Parameter Estimation Problem

$$\theta_k^* \in \arg \min_{\theta} J_k^{\text{id}}$$

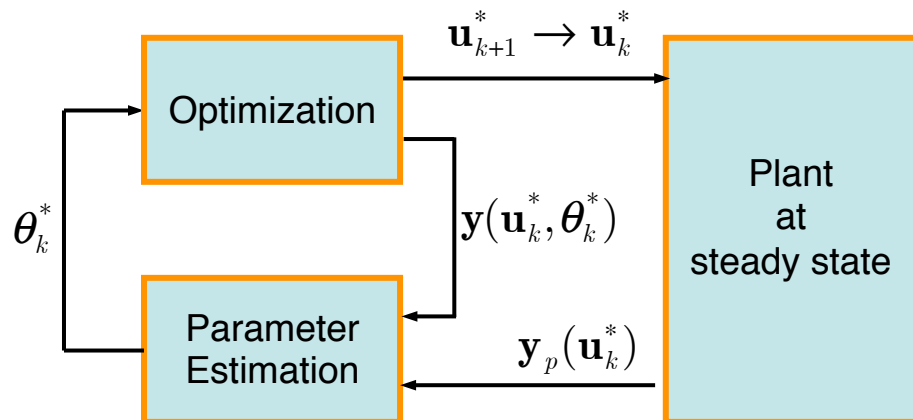
$$J_k^{\text{id}} = \left[ \mathbf{y}_p(\mathbf{u}_k^*) - \mathbf{y}(\mathbf{u}_k^*, \theta) \right]^T \mathbf{Q} \left[ \mathbf{y}_p(\mathbf{u}_k^*) - \mathbf{y}(\mathbf{u}_k^*, \theta) \right]$$

## Optimization Problem

$$\mathbf{u}_{k+1}^* \in \arg \min_{\mathbf{u}} \phi(\mathbf{u}, \mathbf{y}(\mathbf{u}, \theta_k^*))$$

$$\text{s.t.} \quad \mathbf{g}(\mathbf{u}, \mathbf{y}(\mathbf{u}, \theta_k^*)) \leq \mathbf{0}$$

$$\mathbf{u}^L \leq \mathbf{u} \leq \mathbf{u}^U$$

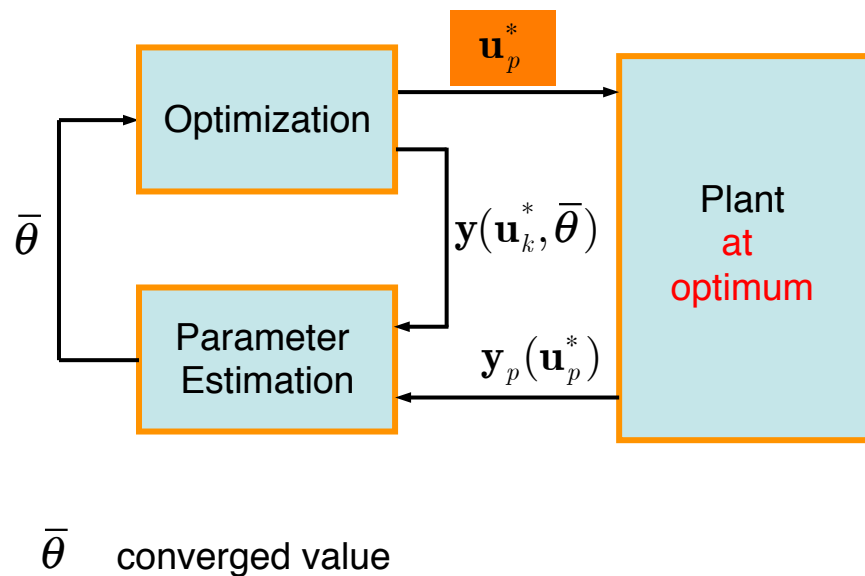


Current Industrial Practice  
for tracking the changing optimum  
in the presence of disturbances

T.E. Marlin, A.N. Hrymak. Real-Time Operations Optimization of Continuous Processes,  
*AIChE Symposium Series - CPC-V*, **93**, 156-164, 1997

# Model Adequacy for Two-Step Approach

A process model is said to be adequate for use in an RTO scheme if it is capable of producing a fixed point for that RTO scheme **at the plant optimum**



## Model-adequacy conditions

$\frac{\partial J^{\text{id}}}{\partial \theta} \left( \mathbf{y}_p(\mathbf{u}_p^*), \mathbf{y}(\mathbf{u}_p^*, \bar{\theta}) \right) = 0,$	} Par. Est.
$\frac{\partial^2 J^{\text{id}}}{\partial \theta^2} \left( \mathbf{y}_p(\mathbf{u}_p^*), \mathbf{y}(\mathbf{u}_p^*, \bar{\theta}) \right) > 0,$	
$G_i(\mathbf{u}_p^*, \bar{\theta}) = 0, \quad i \in A(\mathbf{u}_p^*)$	} Opt.
$G_i(\mathbf{u}_p^*, \bar{\theta}) < 0, \quad i \notin A(\mathbf{u}_p^*)$	
$\nabla_r \Phi(\mathbf{u}_p^*, \bar{\theta}) = 0,$	
$\nabla_r^2 \Phi(\mathbf{u}_p^*, \bar{\theta}) > 0$	

J.F. Forbes, T.E. Marlin. Design Cost: A Systematic Approach to Technology Selection for Model-Based Real-Time Optimization Systems. *Comp. Chem. Eng.*, **20**(6/7), 717-734, 1996

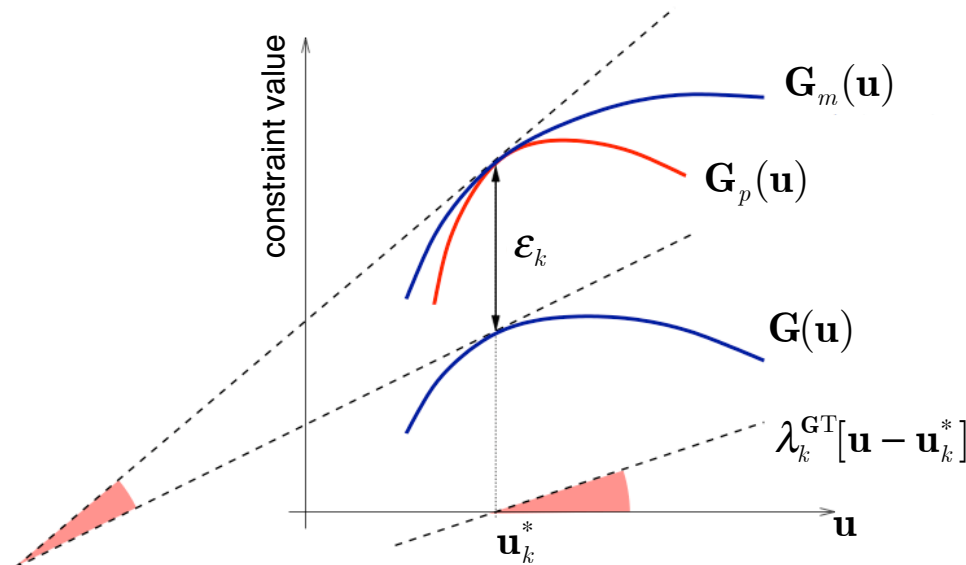


## 2. Adaptation of Cost & Constraints Input-Affine Correction to the Model

### Modified Optimization Problem

$$\begin{aligned} \mathbf{u}_{k+1}^* \in \arg \min_{\mathbf{u}} \quad & \Phi_m(\mathbf{u}) := \Phi(\mathbf{u}) + \lambda_k^{\Phi T} [\mathbf{u} - \mathbf{u}_k^*] \\ \text{s.t.} \quad & \mathbf{G}_m(\mathbf{u}) := \mathbf{G}(\mathbf{u}) + \boldsymbol{\varepsilon}_k + \lambda_k^{GT} [\mathbf{u} - \mathbf{u}_k^*] \leq 0 \\ & \mathbf{u}^L \leq \mathbf{u} \leq \mathbf{u}^U \end{aligned}$$

Affine corrections of  
cost and constraint  
functions



Force the modified problem  
to satisfy the optimality  
conditions of the **plant**

P.D. Roberts and T.W. Williams, On an Algorithm for Combined System Optimization and Parameter Estimation, *Automatica*, **17**(1), 199–209, 1981

# Input-Affine Correction to the Model

## Modified Optimization Problem

$$\begin{aligned} \mathbf{u}_{k+1}^* \in \arg \min_{\mathbf{u}} \quad & \Phi_m(\mathbf{u}) := \Phi(\mathbf{u}) + \lambda_k^{\Phi^T} [\mathbf{u} - \mathbf{u}_k^*] \\ \text{s.t.} \quad & \mathbf{G}_m(\mathbf{u}) := \mathbf{G}(\mathbf{u}) + \varepsilon_k + \lambda_k^{G^T} [\mathbf{u} - \mathbf{u}_k^*] \leq 0 \\ & \mathbf{u}^L \leq \mathbf{u} \leq \mathbf{u}^U \end{aligned}$$

- KKT Elements:  $\mathcal{C}^T = \left( G_1, \dots, G_{n_g}, \frac{\partial G_1}{\partial \mathbf{u}}, \dots, \frac{\partial G_{n_g}}{\partial \mathbf{u}}, \frac{\partial \Phi}{\partial \mathbf{u}} \right) \in \mathbb{R}^{n_K} \quad n_K = n_g + n_u(n_g + 1)$
- KKT Modifiers:  $\Lambda^T = \left( \varepsilon_1, \dots, \varepsilon_{n_g}, \lambda^{G_1^T}, \dots, \lambda^{G_{n_g}^T}, \lambda^{\Phi^T} \right) \in \mathbb{R}^{n_K}$

## Modifier Adaptation (without filter)

$$\Lambda_k = C_p(\mathbf{u}_k^*) - C(\mathbf{u}_k^*)$$

Requires evaluation of  
KKT elements of plant

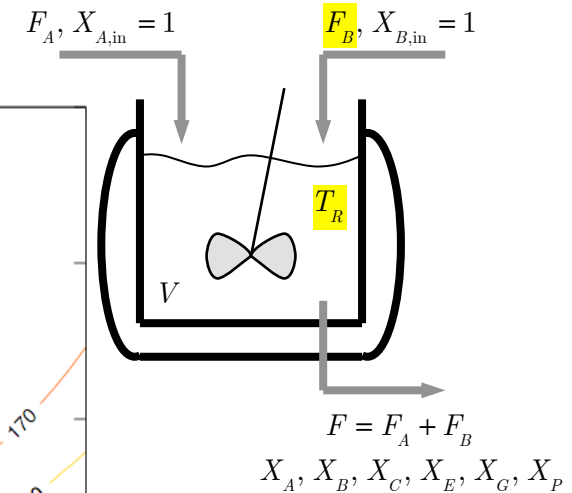
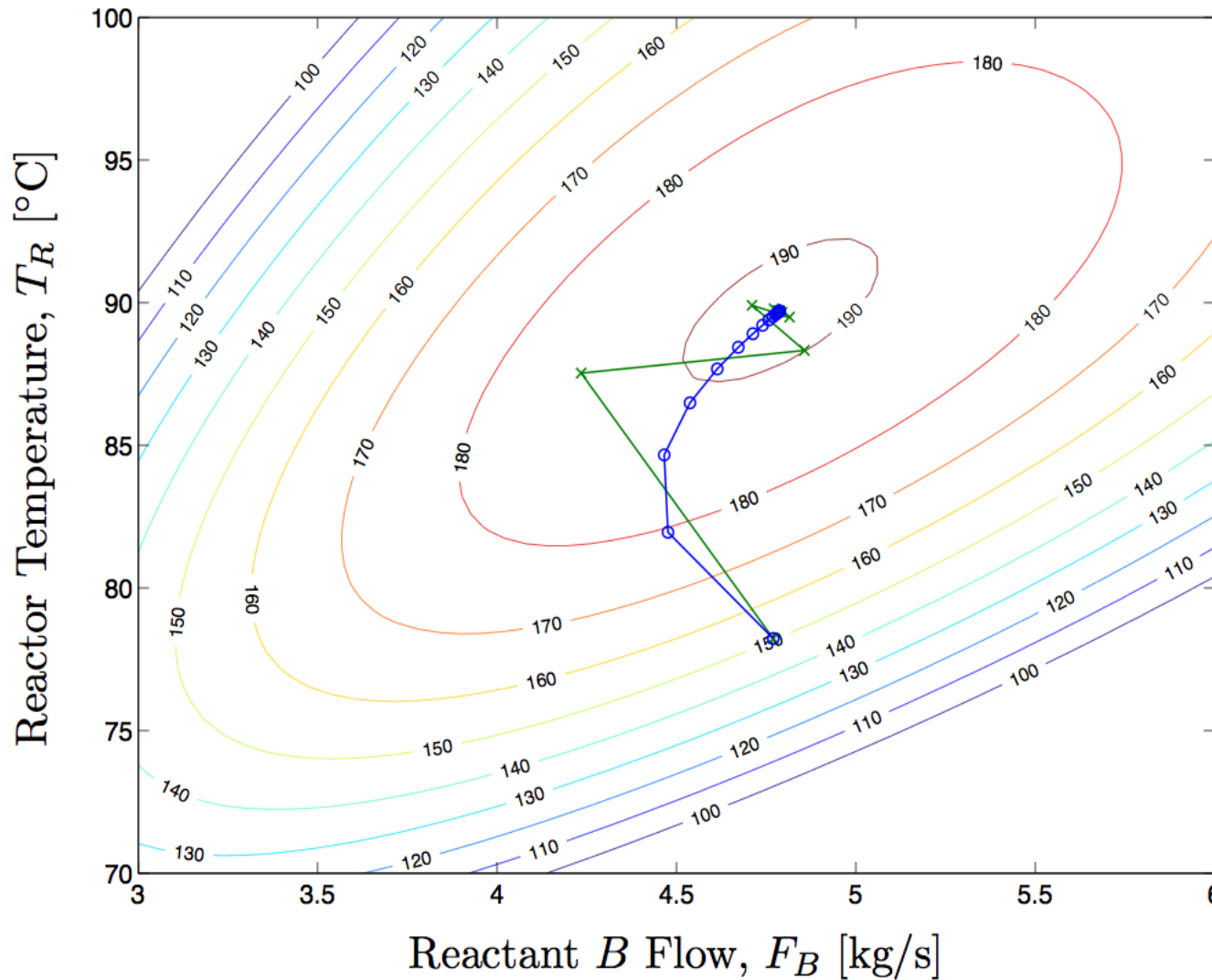
## Modifier Adaptation (with filter)

$$\Lambda_k = (\mathbf{I} - \mathbf{K}) \Lambda_{k-1} + \mathbf{K} [C_p(\mathbf{u}_k^*) - C(\mathbf{u}_k^*)]$$

W. Gao and S. Engell, Iterative Set-point Optimization of Batch Chromatography, *Comput. Chem. Eng.*, **29**, 1401–1409, 2005  
A. Marchetti, B. Chachuat and D. Bonvin, Modifier-Adaptation Methodology for Real-Time Optimization, *I&EC Research*, **48**(13), 6022-6033 (2009)

# Example Revisited

Modifier adaptation



Williams-Otto Reactor

- 4<sup>th</sup>-order model
- 2 inputs
- 2 adjustable par.

Converges to plant  
optimum

# Modeling for Optimization

## Features of a “good” model

- Must be able to predict the optimality conditions of the plant:  
**active constraints and (reduced) gradients**
- Focuses on the optimal solution  
→ **“solution model”** rather than “plant model”

## Need to be able to estimate the plant gradients

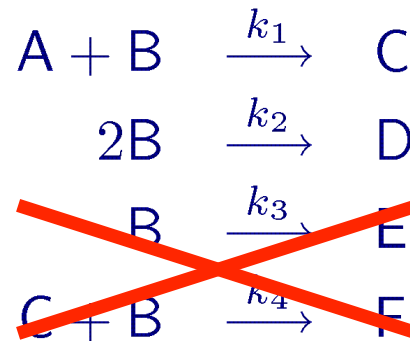
- From cost and constraint values at previous operating points
- Must be able to use the key measurements (active constraints and gradients)

# Run-to-Run Optimization of Semi-Batch Reactor

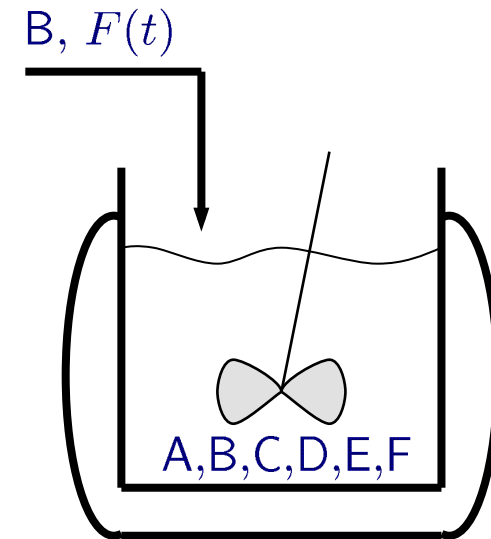
## Industrial Reaction System

**Lonza**

*Simulated  
Reality*



*Model*



Manipulated Variables:  $F(t)$  (feed flow rate of B)

Objective: **Maximize**  $n_C(t_f)$  (production of C)

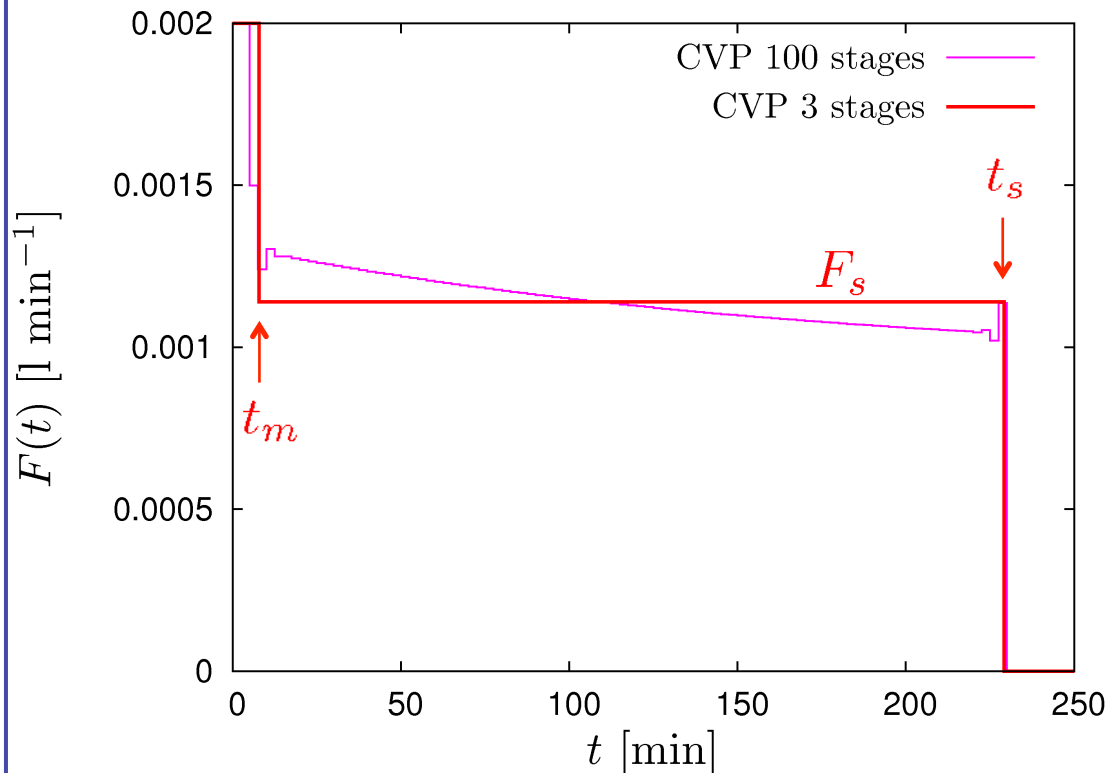
Constraints:

**Input bounds:**  $0 \leq F(t) \leq 0.002 \text{ l min}^{-1}$

**Terminal constraints:**  $c_B(t_f) \leq 0.025 \text{ mol l}^{-1}$  (max. residual concentration)

$c_D(t_f) \leq 0.15 \text{ mol l}^{-1}$  (max. by-product concentration)

# Nominal Optimal Input



## Plant model

- 3 nonlinear balance equations
- 2 uncertain parameters  $k_1$  and  $k_2$
- Measurements to adjust  $k_1$  and  $k_2$

## A solution model

- 3 arcs:  $F_{\max}$ ,  $F_s$  and  $F_{\min}$
- 3 adjustable parameters  $t_m$ ,  $t_s$  and  $F_s$
- Measurements to adjust  $t_m$ ,  $t_s$  and  $F_s$

### Optimal Solution

3 arcs, 2 active terminal constraints

$$J^* \approx 0.5081 \text{ mol}$$

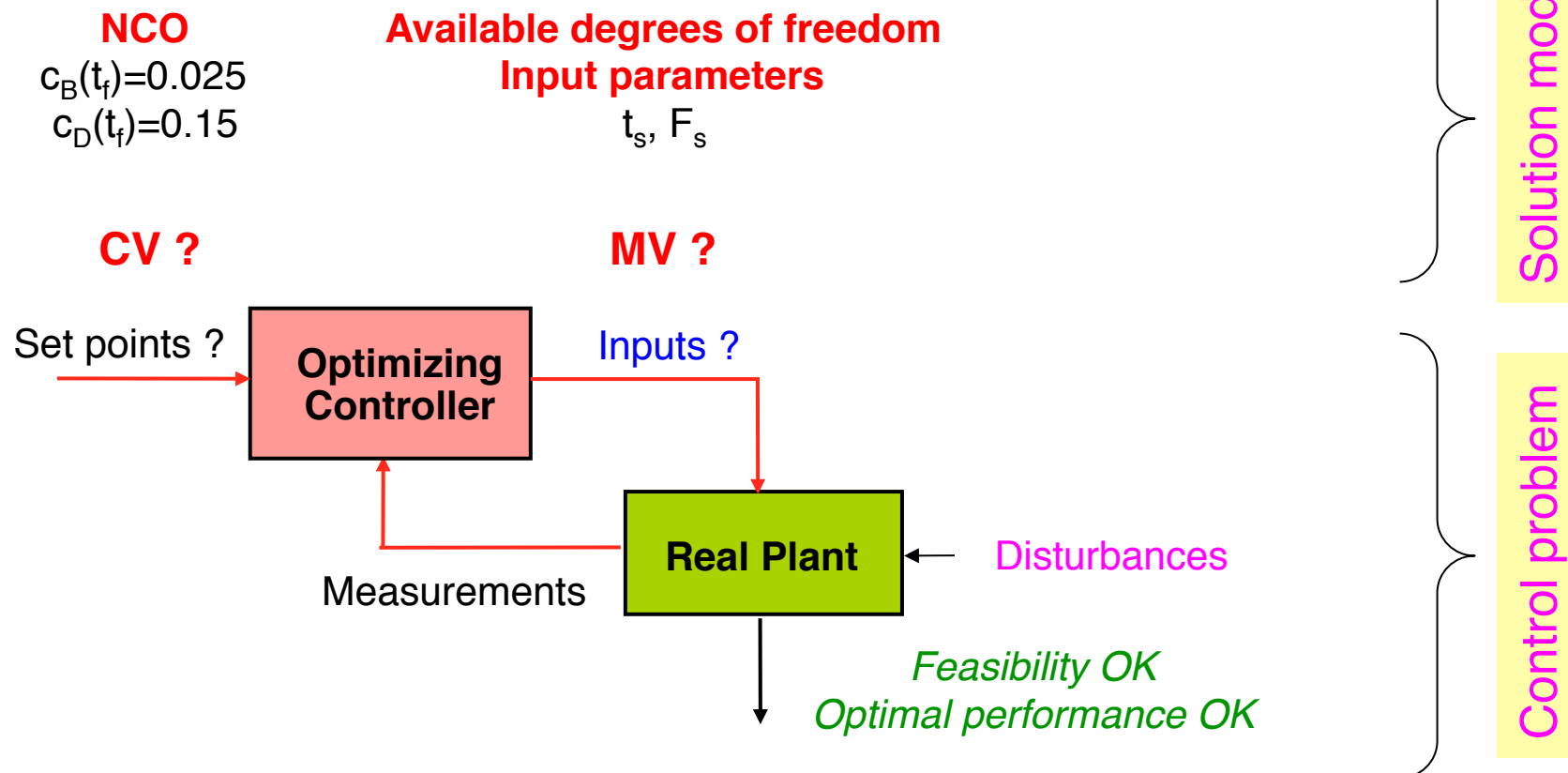
### Approximate Solution

Parameterization:  $\mathbf{u} = (t_m, t_s, F_s)$

$$J^* \approx 0.5079 \text{ mol}$$



### 3. Adaptation of Inputs NCO tracking



B. Srinivasan and D. Bonvin, Real-Time Optimization of Batch Processes by Tracking the Necessary Conditions of Optimality, I&EC Research, 46, 492-504 (2007).

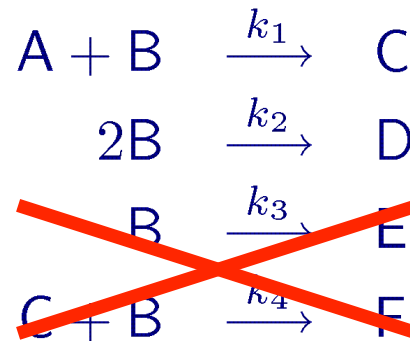
# Comparison of RTO Schemes

## Run-to-Run Optimization of Semi-Batch Reactor

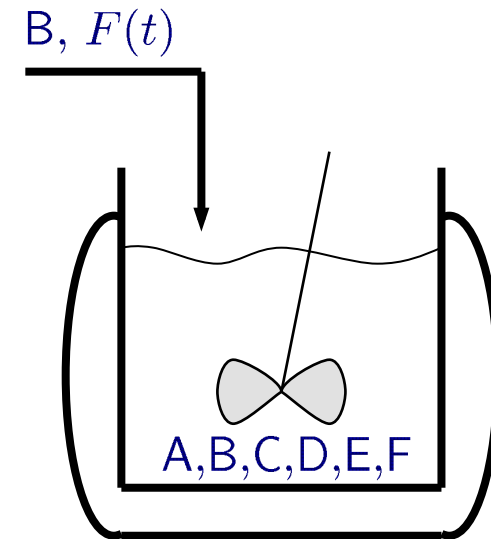
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Manipulated Variables:  $F(t)$  (feed flow rate of B)

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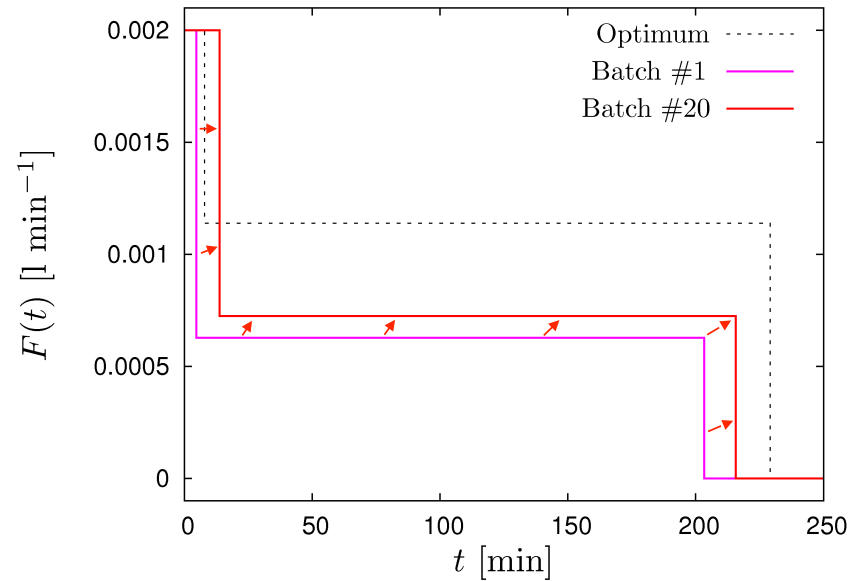
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$c_D(t_f) \leq 0.15 \text{ mol l}^{-1}$  (max. by-product concentration)

# Adaptation of Model Parameters $k_1$ and $k_2$



- Measurement Noise:  $\sigma_y = 5\%$   
(10% constraint backoffs)

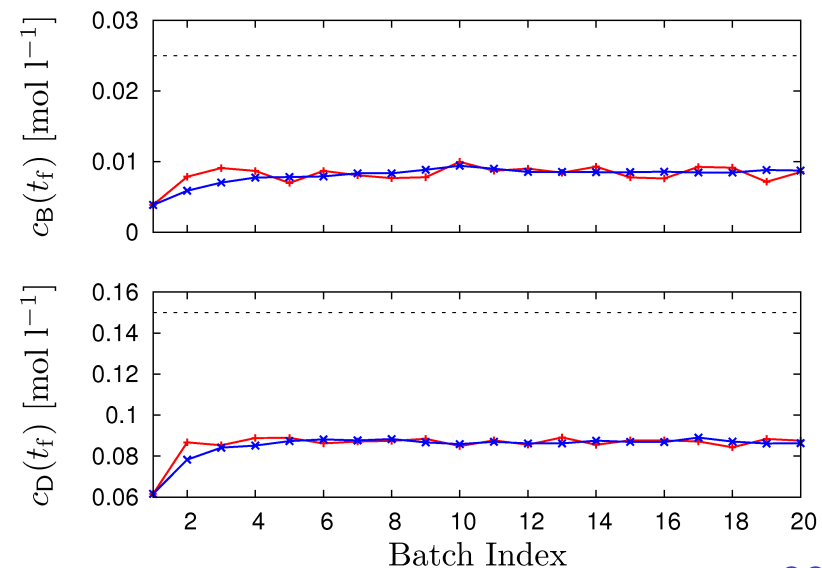
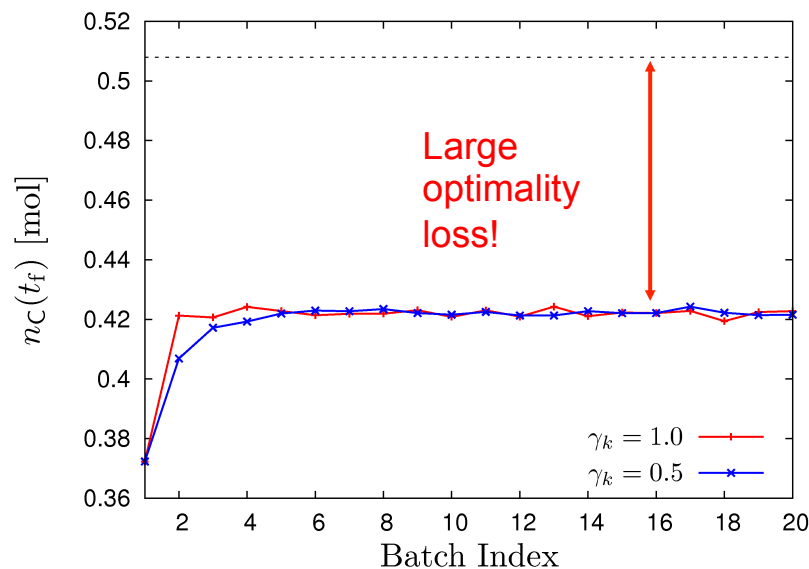
- Identification Objective:

$$J^{\text{id}} = \sum_{k=1}^{n^{\text{meas}}} \left[ \frac{y - y^{\text{meas}}}{\bar{y}} \right]_{t=t_k}^2, \quad y = (c_B, c_C, c_D)$$

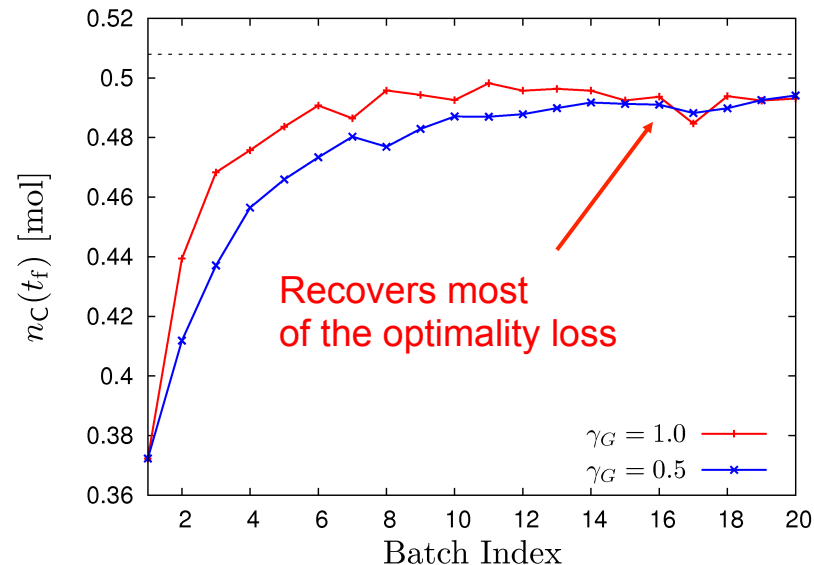
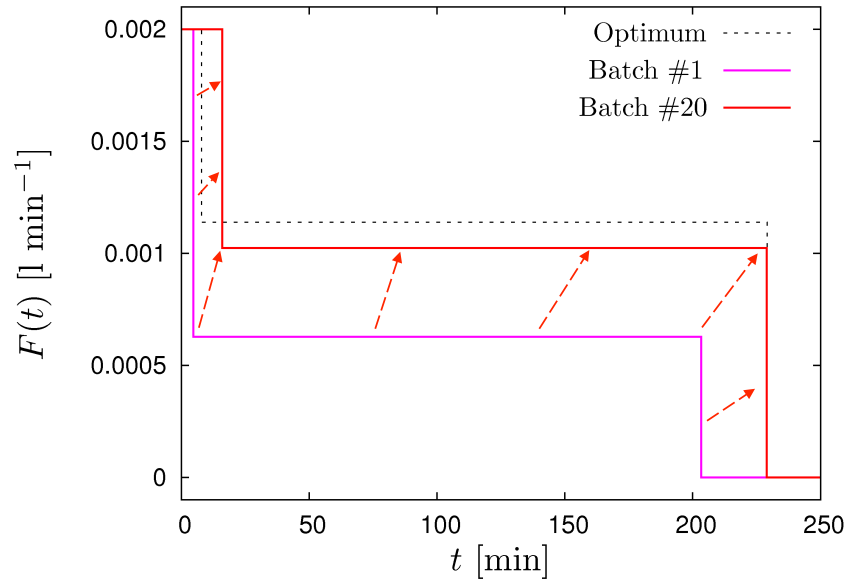
$n^{\text{meas}} = 6$

- Exponential Filter for  $k_1, k_2$ :

$$\begin{pmatrix} k_1^i \\ k_2^i \end{pmatrix} = (1 - \gamma_k) \begin{pmatrix} k_1^{i-1} \\ k_2^{i-1} \end{pmatrix} + \gamma_k \begin{pmatrix} k_1^* \\ k_2^* \end{pmatrix}$$



# Adaptation of Constraint Modifiers $\varepsilon_G$

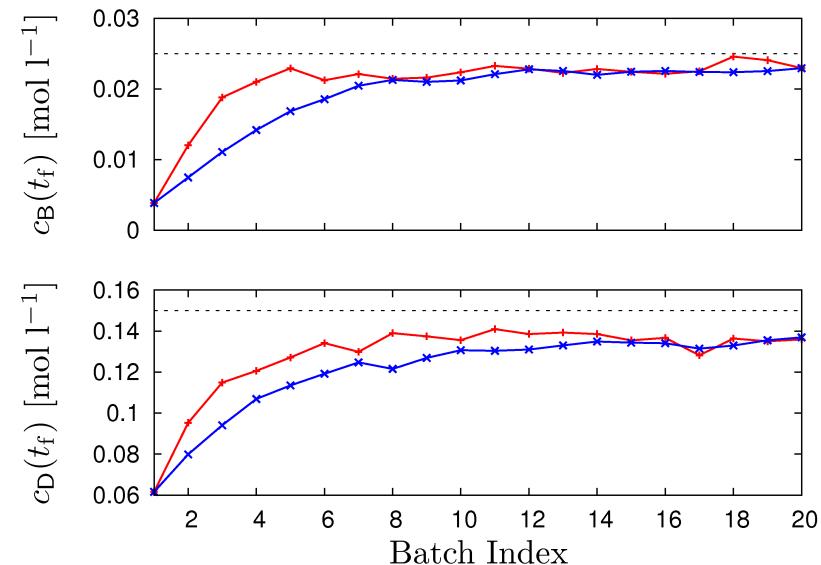


- Measurement Noise:  $\sigma_y = 5\%$   
(10% constraint backoffs)

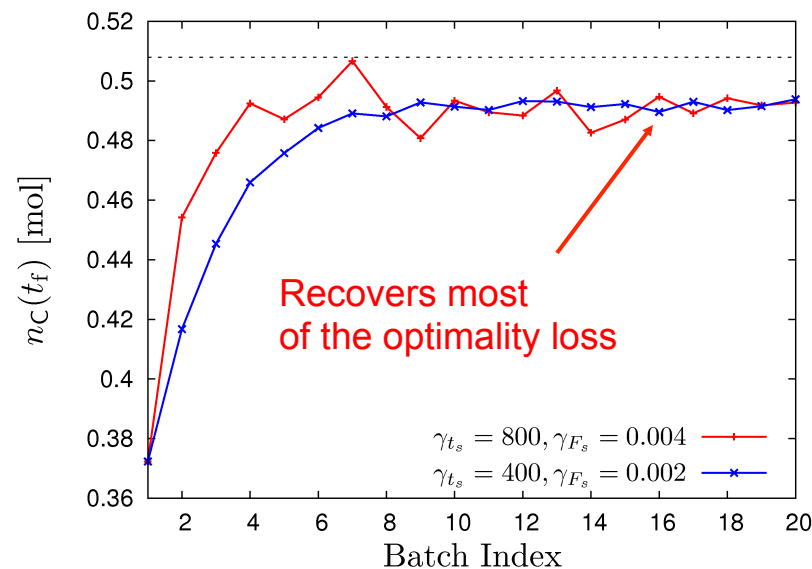
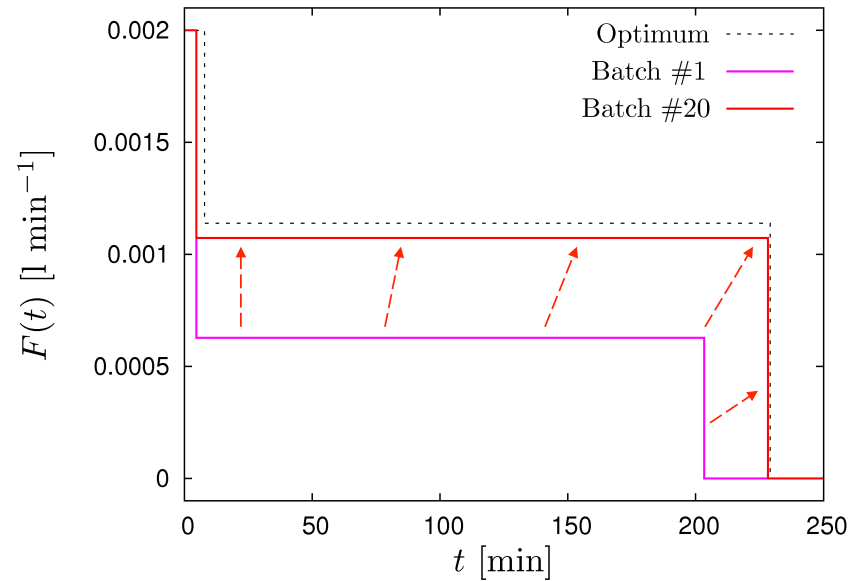
- No Gradient Correction

- Exponential Filter for Modifiers:

$$\begin{pmatrix} \varepsilon_{G,1}^i \\ \varepsilon_{G,2}^i \end{pmatrix} = (1 - \gamma_G) \begin{pmatrix} \varepsilon_{G,1}^{i-1} \\ \varepsilon_{G,2}^{i-1} \end{pmatrix} + \gamma_G \begin{pmatrix} c_B^{\text{meas}}(t_f) - c_B(t_f) \\ c_D^{\text{meas}}(t_f) - c_D(t_f) \end{pmatrix}_{\pi=\pi^{i-1}}$$



# Adaptation of Input Parameters $t_s$ and $F_s$



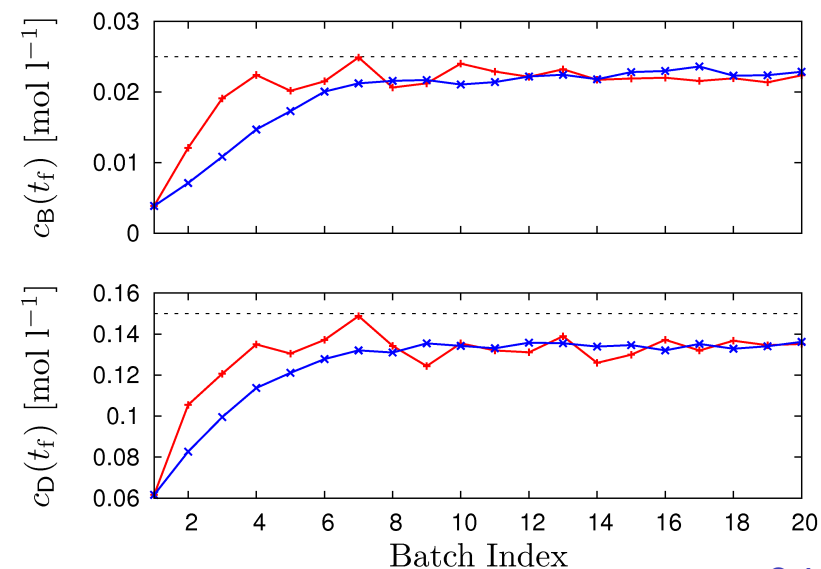
- Measurement Noise:  $\sigma_y = 5\%$   
(10% constraint back-offs)

- No Gradient Correction

- Controller Design:

$$t_m = 4.71 \text{ min (fixed)}$$

$$\begin{pmatrix} t_s^k \\ F_s^k \end{pmatrix} = \begin{pmatrix} t_s^{k-1} \\ F_s^{k-1} \end{pmatrix} + \begin{pmatrix} \gamma_{t_s} \\ \gamma_{F_s} \end{pmatrix} \begin{pmatrix} c_B^{\text{meas}}(t_f) - 0.025 \\ c_D^{\text{meas}}(t_f) - 0.15 \end{pmatrix} \pi = \pi^{k-1}$$



# Outline

## What is real-time optimization

- Goal: Optimal plant operation
- Tool: Model-based numerical optimization, experimental optimization
- Key feature: use of real-time measurements

## Real-time optimization framework

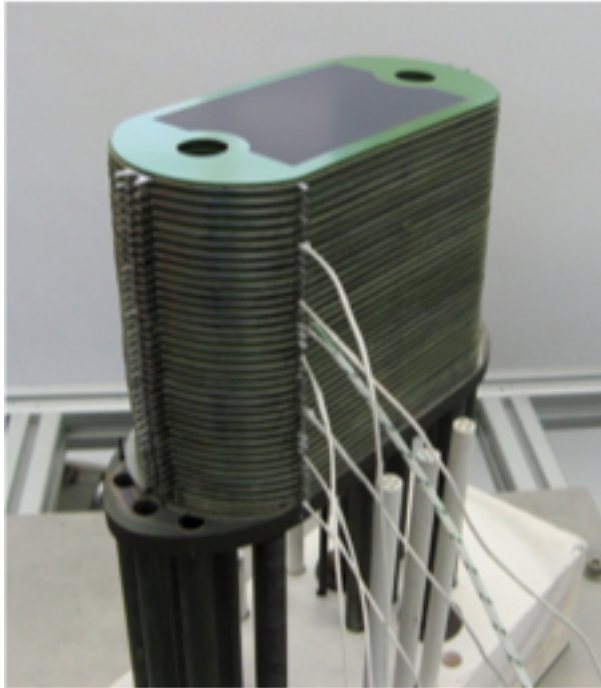
- Three approaches
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- Simulated comparison

## Experimental case studies

- Fuel-cell stack
- Batch polymerization

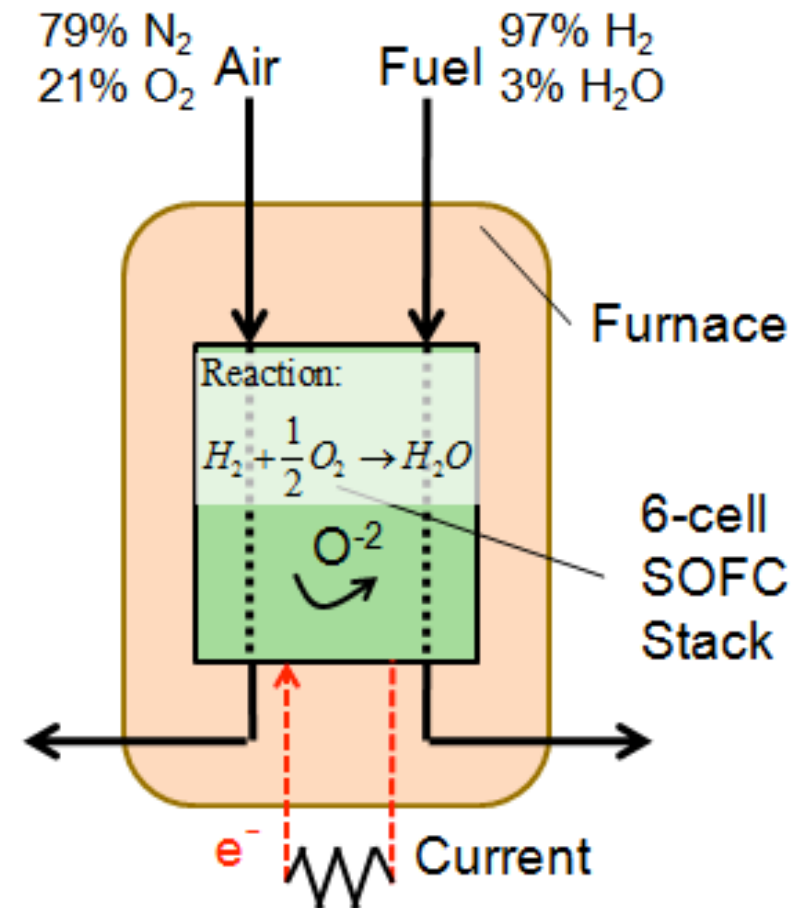


# Solid Oxide Fuel Cell Stack



- Stack of 6 cells, active area of 50 cm<sup>2</sup>, metallic interconnector
- Anodes : standard nickel/yttrium stabilized-zirconia (Ni-YSZ)
- Electrolyte : dense YSZ.
- Cathodes: screen-printed (La, Sr)(Co, Fe)O<sub>3</sub>
- Operation temperatures between 650 and 850°C.

G.A. Bunin, Z. Wullemmin, G. François, A. Nakajo, L. Tsikonis and D. Bonvin, Experimental real-time optimization of a solid oxide fuel cell stack via constraint adaptation, *Energy*, **39**(1), 54-62 (2012).

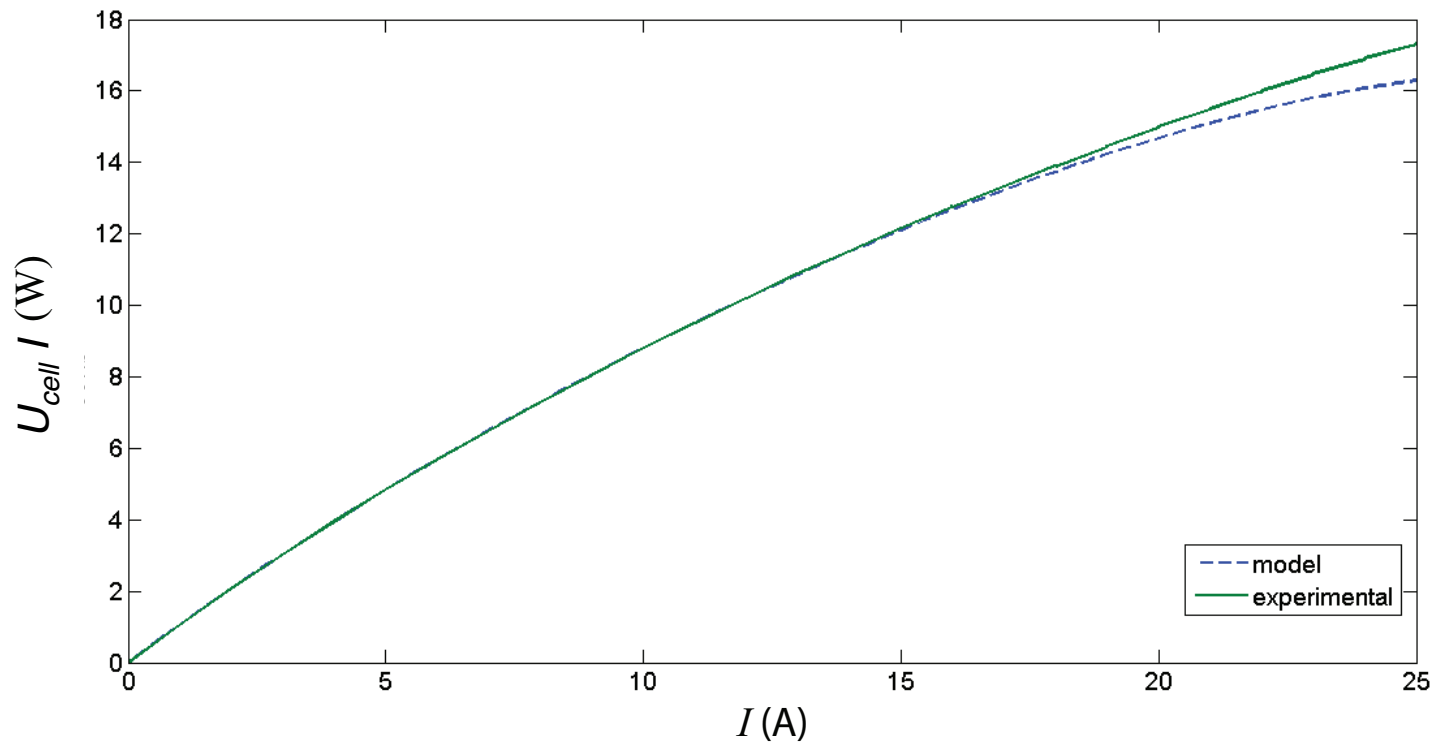


# RTO via Constraint Adaptation

## Experimental features

- Inputs: flowrates ( $H_2$ ,  $O_2$ ), current (or load)
- Outputs: power density, cell potential, electrical efficiency
- Time-scale separation
  - *slow temperature dynamics, treated as process drift !*
  - *static model (for the rest)*
- Power demand changes without prior knowledge
- Inaccurate model in the operating region (power, cell)

# RTO via Constraint Adaptation



**Challenge:** Implement optimal operation with changing power demand

# RTO via Constraint Adaptation

## Problem Formulation

At each RTO instant  $k$ , solve a static optimization problem, with a zeroth-order modifier in the constraints, **regardless of the fact that  $T$  has reached steady state or not**

$$\max_{u_k} \eta(\mathbf{u}_k, \Theta)$$

$$\text{s.t.} \quad p_{\text{el}}(\mathbf{u}_k, \Theta) + \varepsilon_{k-1}^{p_{\text{el}}} = p_{\text{el}}^S$$

$$U_{\text{cell}}(\mathbf{u}_k, \Theta) + \varepsilon_{k-1}^{U_{\text{cell}}} \geq 0.75 \text{ V}$$

$$v(\mathbf{u}_k) \leq 0.75$$

$$4 \leq 2 \frac{u_{2,k}}{u_{1,k}} = \lambda_{\text{air}}(\mathbf{u}_k) \leq 7$$

$$u_{1,k} \geq 3.14 \text{ mL}/(\text{min cm}^2)$$

$$u_{3,k} \leq 30 \text{ A}$$

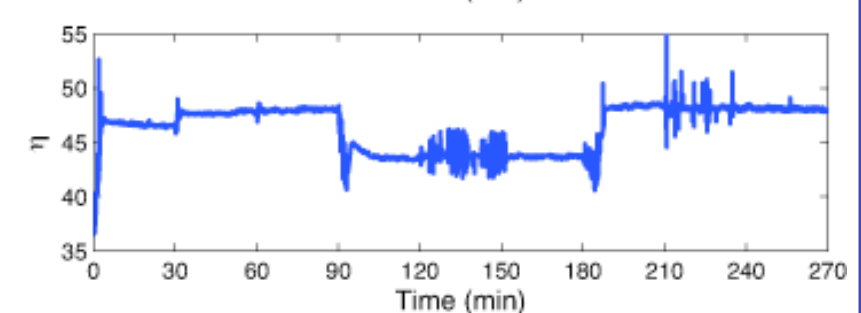
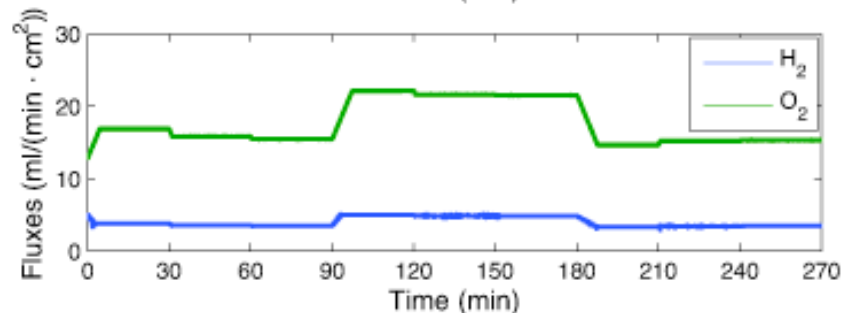
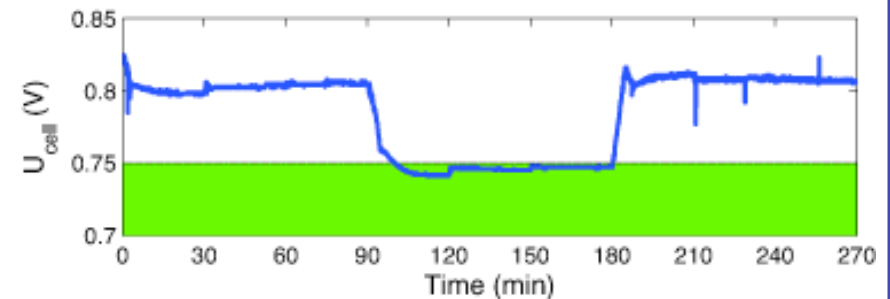
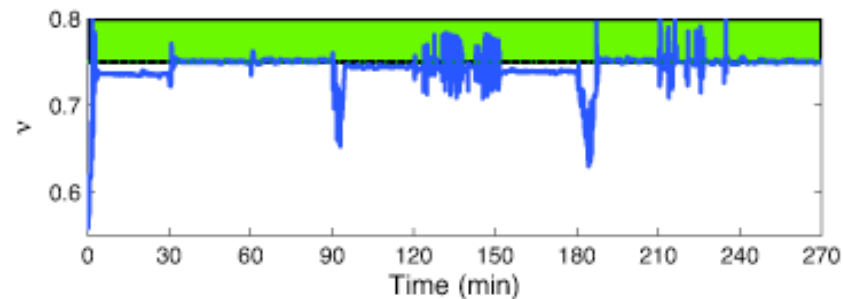
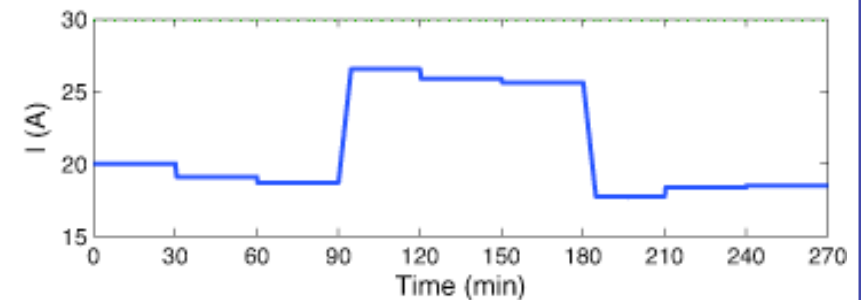
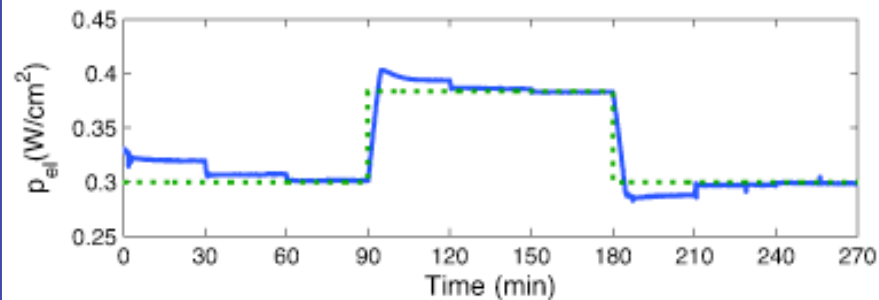
$$u_k = \begin{bmatrix} u_{1,k} = \dot{n}_{\text{H}_2,k} \\ u_{2,k} = \dot{n}_{\text{O}_2,k} \\ u_{3,k} = I_k \end{bmatrix}$$

$$\varepsilon_k^{p_{\text{el}}} = (1 - K_{p_{\text{el}}}) \varepsilon_{k-1}^{p_{\text{el}}} + K_{p_{\text{el}}} [p_{\text{el,p,k}} - p_{\text{el}}(\mathbf{u}_k, \Theta)]$$

$$\varepsilon_k^{U_{\text{cell}}} = (1 - K_{U_{\text{cell}}}) \varepsilon_{k-1}^{U_{\text{cell}}} + K_{U_{\text{cell}}} [U_{\text{cell,p,k}} - U_{\text{cell}}(\mathbf{u}_k, \Theta)]$$

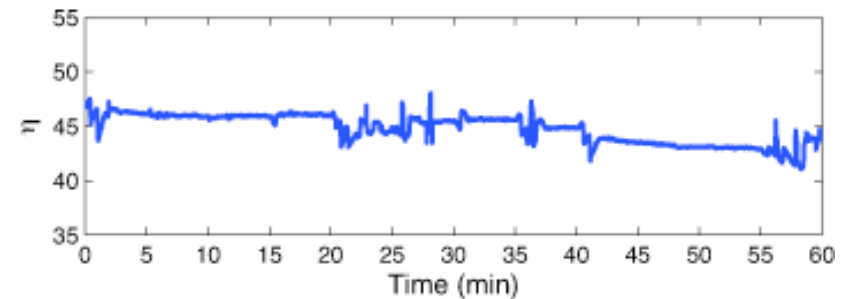
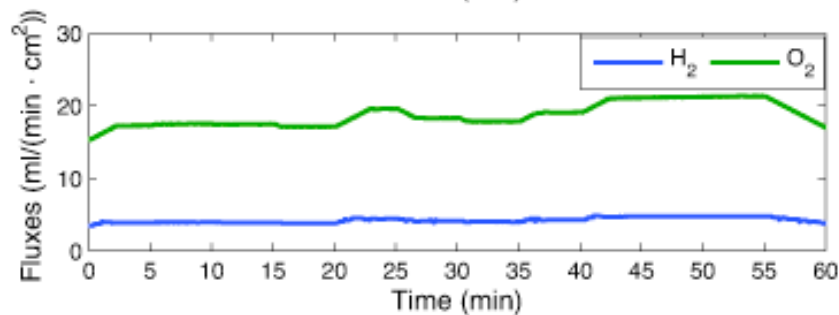
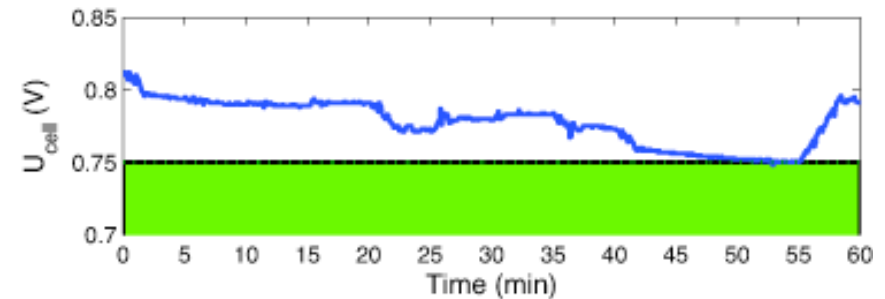
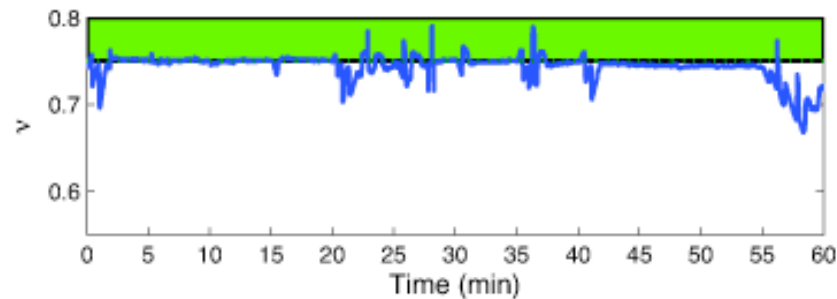
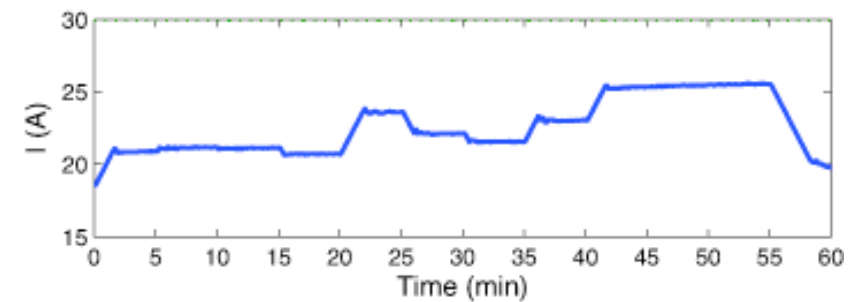
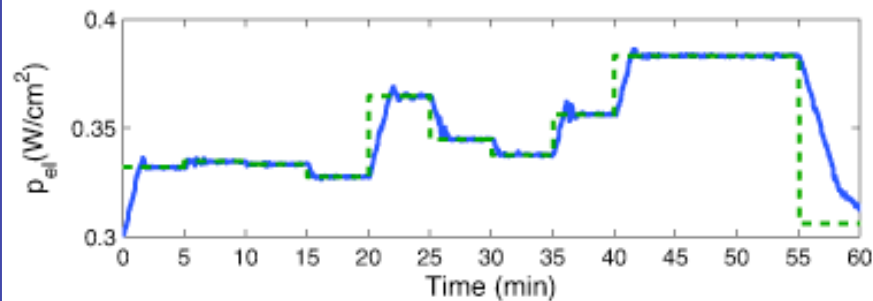
# Slow RTO (“Wait for Steady State”)

- RTO very 30 min
- Unknown power changes every 90 min



# Fast RTO with Random Power Changes

- Use steady-state model for predicting temperature
- RTO every 10 s, load changes every 5 min

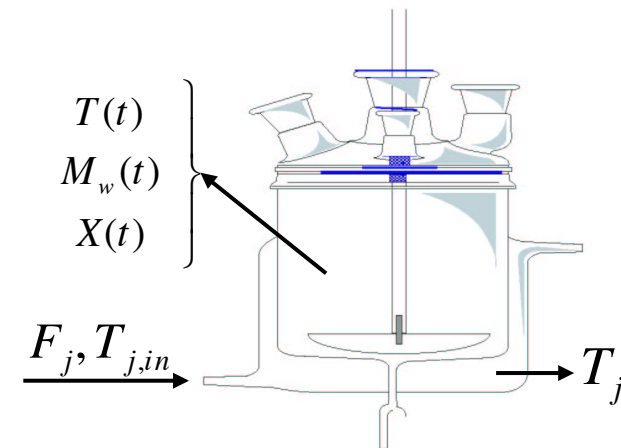




# Emulsion Copolymerization Process

## ■ Industrial process

- 1-ton reactor, risk of runaway
- Initiator efficiency can vary considerably
- Several recipes
  - *different initial conditions*
  - *different initiator feeding policies*
  - *use of chain transfer agent*

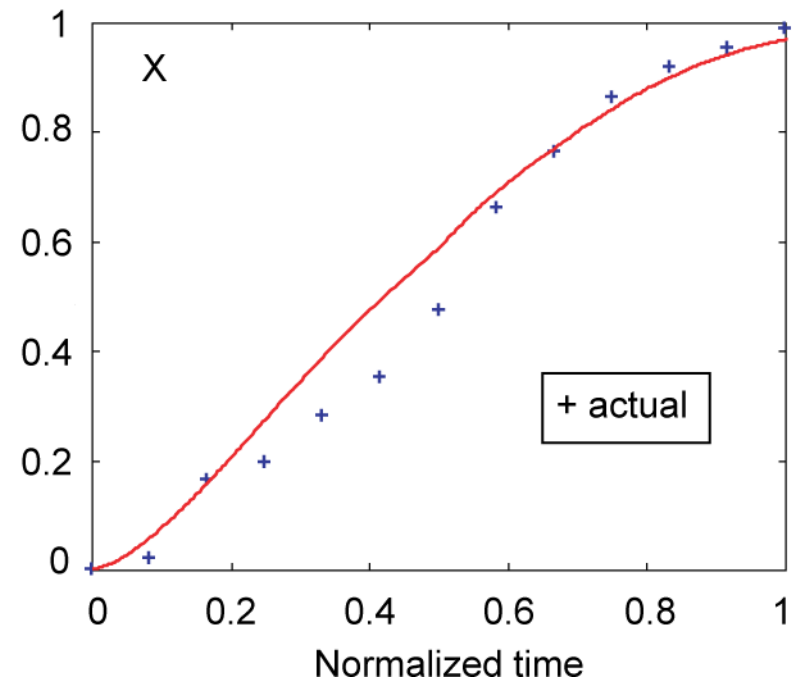
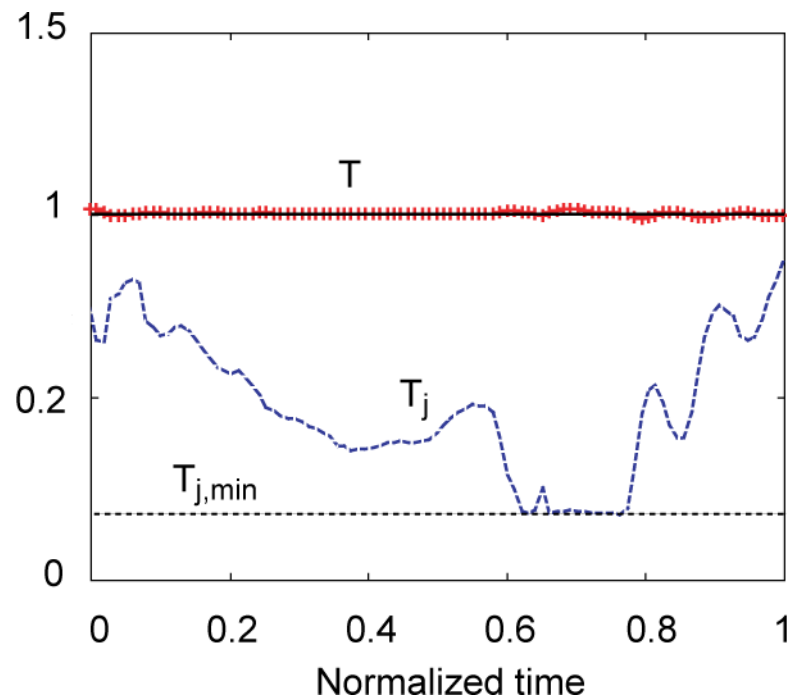


- Modeling difficulties
- Uncertainty

## ■ Objective: Minimize **batch time** by adjusting the reactor temperature

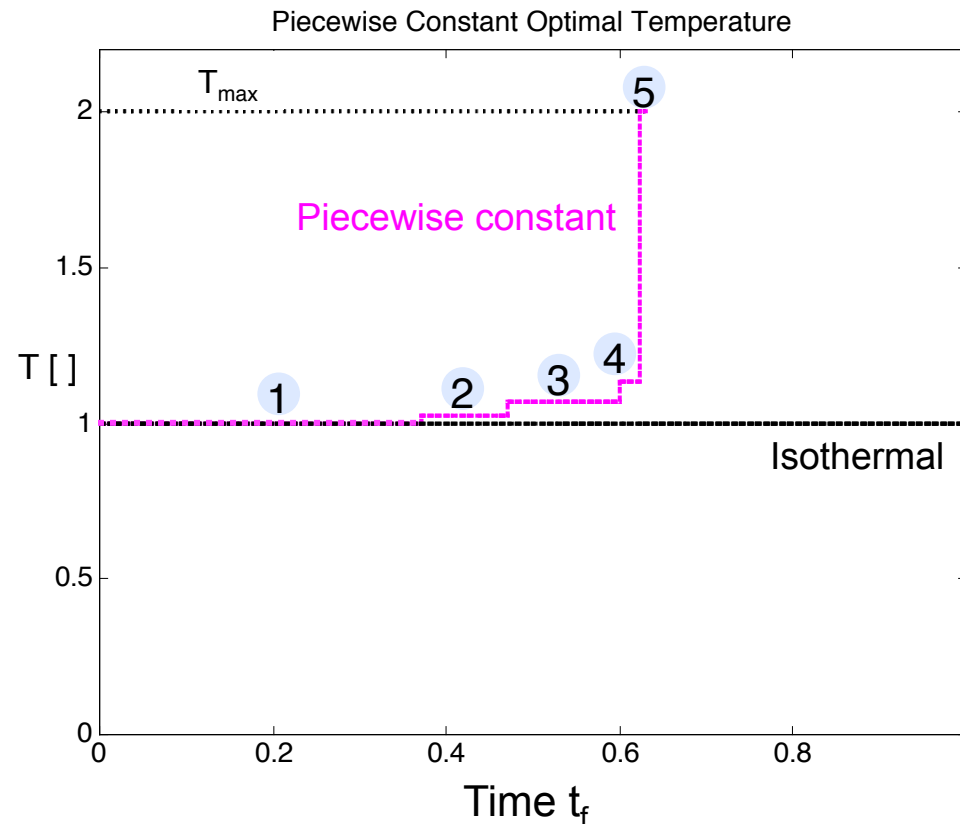
- Temperature and heat removal constraints
- Quality constraints at final time

# Industrial Practice



# Optimal Temperature Profile

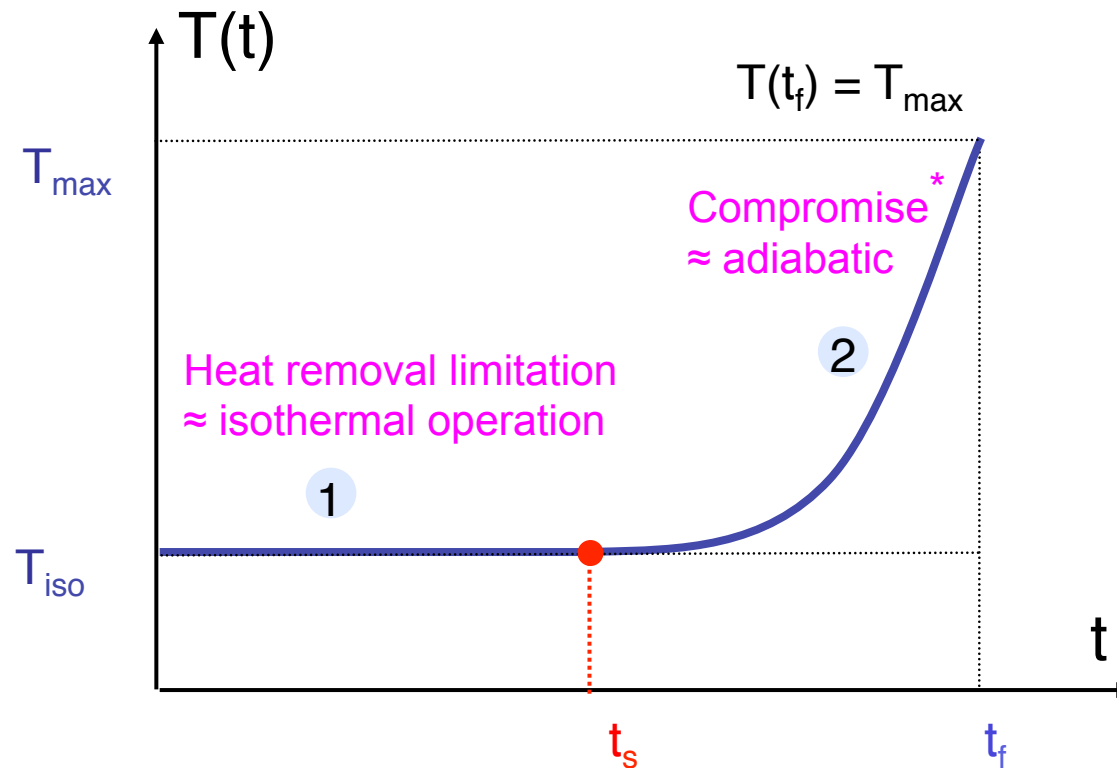
## Numerical Solution using a Tendency Model



- Current practice: isothermal
- Numerical optimization
  - ✓ Piecewise-constant input
  - ✓ 5 decision variables ( $T_2$ - $T_5$ ,  $t_f$ )
  - ✓ Fixed relative switching times
- Active constraints
  - ✓ Interval 1: heat removal
  - ✓ Interval 5:  $T_{\max}$

# Model of the Solution

## Semi-adiabatic Profile

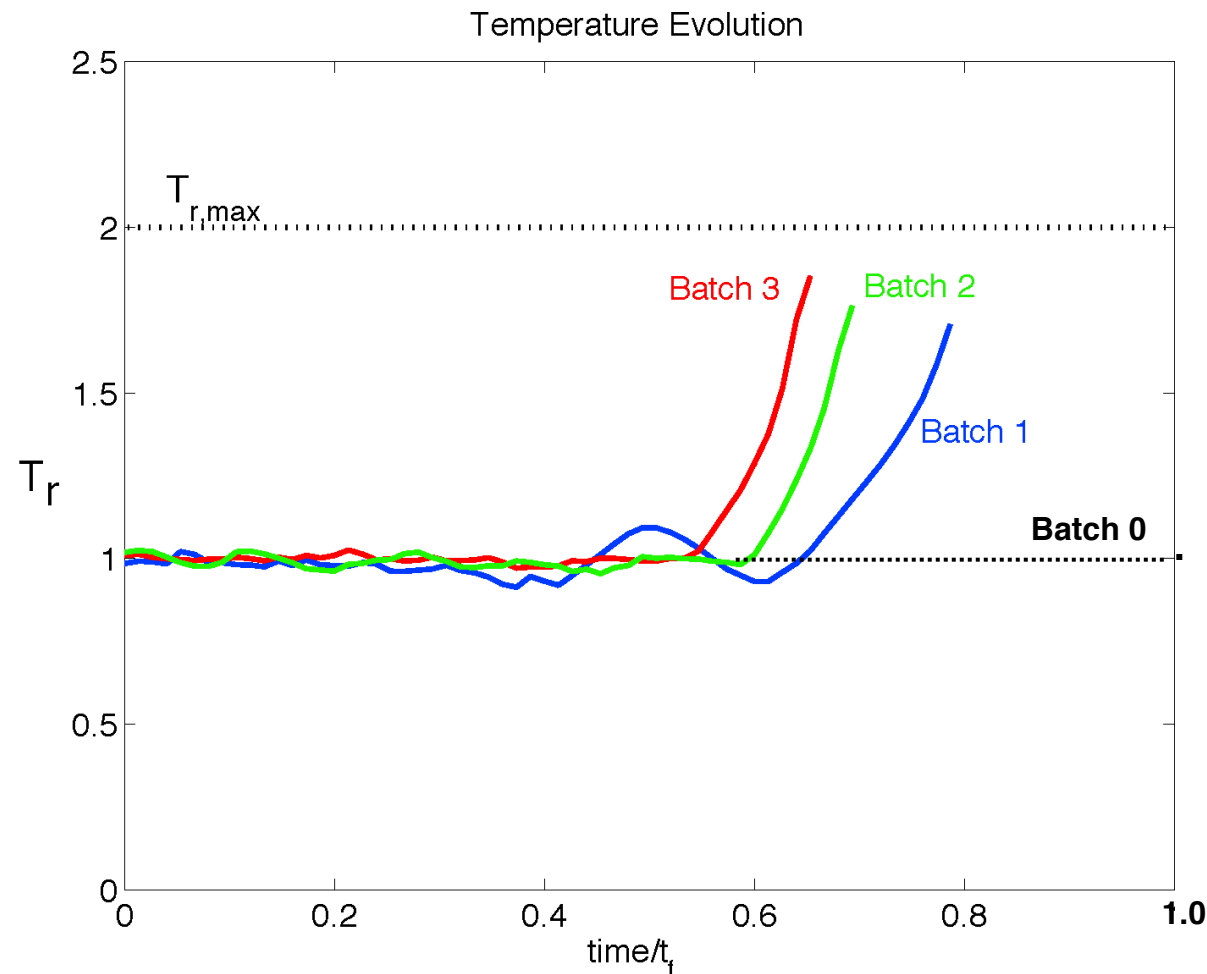


\* Compromise between conversion and quality

$t_s$  enforces  $T(t_f) = T_{max}$

run-to-run adjustment of  $t_s$

# Industrial Results with NCO Tracking



**AQUA+TECH**  
SPECIALTIES SA

1-ton reactor

Final time

- Isothermal: 1.00
- Batch 1: 0.78
- Batch 2: 0.72
- Batch 3: 0.65

Francois *et al.*, Run-to-run Adaptation of a Semi-adiabatic Policy for the Optimization of an Industrial Batch Polymerization Process, *I&EC Research*, **43**(23), 7238-7242, 2004

# Conclusions

## Process optimization is difficult in practice

- Models are often inaccurate → use real-time measurements
- Repeated estimation and optimization lacks **model adequacy**
- Which measurements? How to best exploit them?  
→ NCO (**active constraints and reduced gradients**)

## Two approaches involving the NCO

- Input-affine corrections to cost and constraints
- NCO tracking (optimization via a multivariable control problem)
- Key challenge is **estimation of plant gradient**

# NCO tracking

## New Paradigm for RTO

### Operator-friendly approach

- Start with best current operation (nominal model-based solution) and **push the process** until constraints are reached
- Know what to manipulate → **solution model**
- Determine how much to change from **measurements**

### Important features

- Two steps: offline (model-based), online (data-driven)
- Can test **robustness** offline by using model perturbations
- Approach converges to **plant optimum**, not model optimum
- Complexity depends on the **number of inputs** (not system order)
- Solution is partly determined by active constraints → easy tracking
- Price to pay: need to **estimate experimental gradients**